

Finite Mixture Models with Applications

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Introduction

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- It concerns modeling a statistical distribution by a mixture (or weighted sum) of other distributions

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- The finite mixture model provides a natural representation of heterogeneity in a finite number of latent classes
- It concerns modeling a statistical distribution by a mixture (or weighted sum) of other distributions
- Finite mixture models are also known as
 - latent class models
 - unsupervised learning models
- Finite mixture models are closely related to
 - intrinsic classification models
 - clustering
 - numerical taxonomy

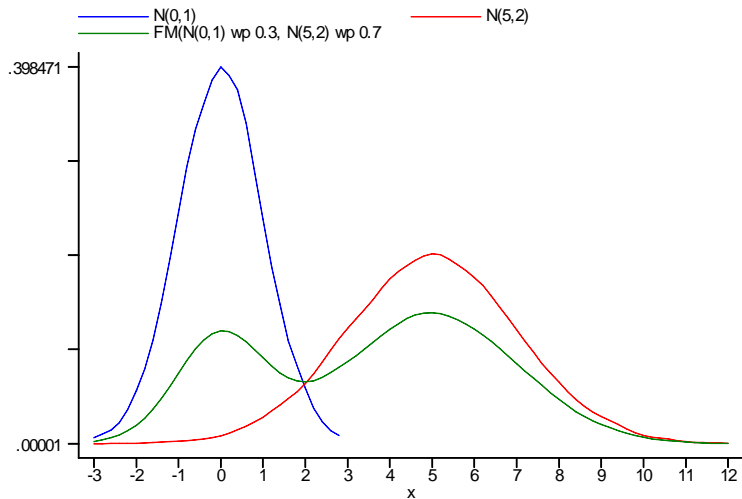
- Heterogeneity of effects for different “classes” of observations
 - wine from different types of grapes
 - healthy and sick individuals
 - normal and complicated pregnancies
 - low and high responses to stress

- Estimating parameters of the distribution of lengths of halibut
- It is known that female halibut is longer, on average, than male fish and that the distribution of lengths is normal
- Gender cannot be determined at measurement
- Then distribution is a 2-component finite mixture of normals

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- It is known that female halibut is longer, on average, than male fish and that the distribution of lengths is normal
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- Then distribution is a 2-component finite mixture of normals
- A finite mixture model allows one to estimate:
 - mean lengths of male and female halibut
 - mixing probability

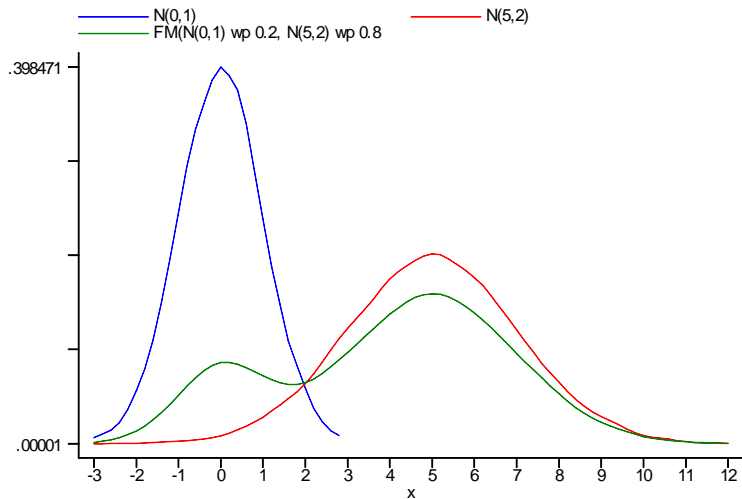
Introduction

A graphical view



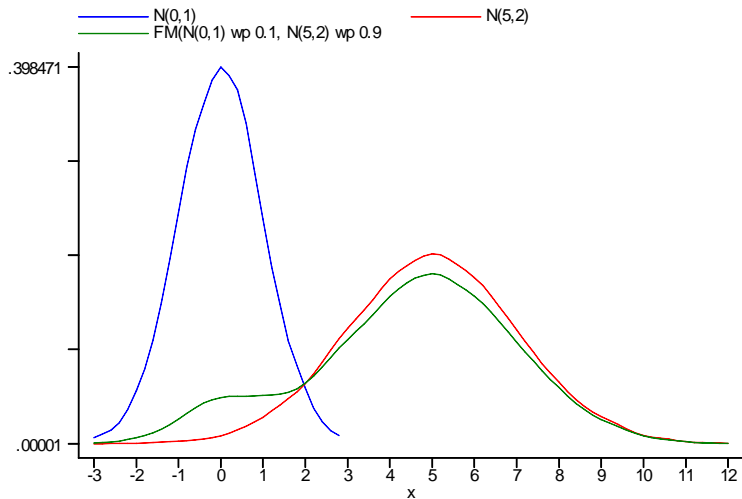
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- Characteristics of wine by cultivar

Introduction

Examples

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- **Public goods experiments - selfish, reciprocal, and altruist**

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- **Models of internet traffic**

Introduction

More generally from a statistical perspective

- FMM is a semiparametric / nonparametric estimator of the density (Lindsay)
- Experience suggests that usually only few latent classes are needed to approximate density well (Heckman)
- In practice FMM are flexible extensions to basic parametric models
 - can generate skewed distributions from symmetric components
 - can generate leptokurtic distributions from mesokurtic ones

Outline of talk

- Introduction

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- Example
 - color of wine

Outline of talk

- Introduction
- Example
 - color of wine
- Model
 - Formulation
 - Estimation
 - Popular densities
 - Properties
 - Model selection
 - Implementation

- Applications

- Birthweight and prenatal care – Conway and Deb, JHE 2005
- Price elasticities of medical care use – Deb and Trivedi, JAE 1997; Deb and Trivedi, JHE 2002
- Effects of job loss on BMI and alcohol consumption – Deb, Gallo, Ayyagari, Fletcher and Sindelar, working paper 2009

- Applications

- Birthweight and prenatal care – Conway and Deb, JHE 2005
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- Conclusions

Example

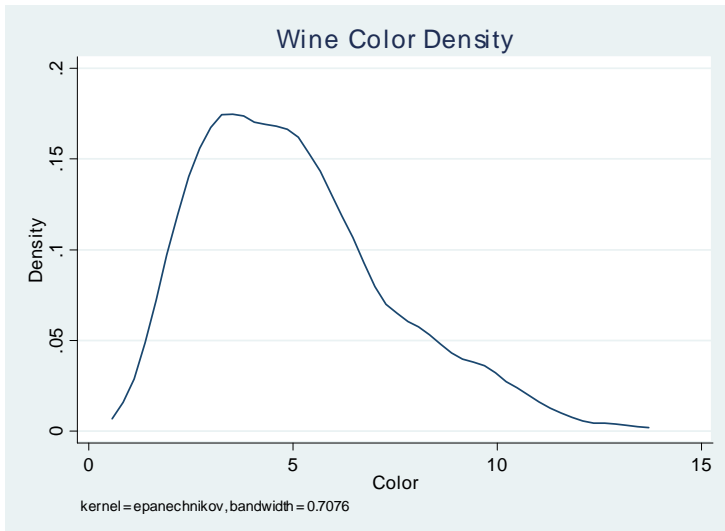
Color of Wine

Results of a chemical analysis of wines grown in the same region in Italy but derived from three different cultivars (grape variety)

Data characteristics			
Cultivar	Freq.	% of total	Color intensity (mean)
1	59	33.15	5.528
2	71	39.89	3.086
3	48	26.97	7.396
Total	178	100	5.058

Example

Color of Wine



Example

Color of Wine

- Finite mixture of Normals with 3 components

$$f(y_i | \theta_1, \theta_2, \dots, \theta_C; \pi_1, \pi_2, \dots, \pi_C) \\ = \sum_{j=1}^C \pi_j \frac{1}{\sqrt{2\pi\sigma_j^2}} \exp\left(-\frac{1}{2\sigma_j^2}(y_i - x_i\beta_j)^2\right)$$

Example

Color of Wine

Estimates from finite mixture of normals with 3 components

Parameter	component 1	component 2	component 3
Constant	4.929 (0.334)	7.548 (0.936)	2.803 (0.244)
π	0.365 (0.176)	0.312 (0.117)	0.323 (0.107)

Data characteristics

Cultivar	Freq.	% of total	Color (mean)
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Example

Color of Wine

Posterior probability (median)

Cultivar	component 1	component 2	component 3
1	0.737	0.195	9.00e-5
2	0.048	0.023	0.923
3	0.030	0.970	7.54e-14

Data characteristics

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- The density function for a C -component finite mixture is

$$f(y|\mathbf{x}; \theta_1, \theta_2, \dots, \theta_C; \pi_1, \pi_2, \dots, \pi_C) = \sum_{j=1}^C \pi_j f_j(y|\mathbf{x}; \theta_j)$$

where $0 < \pi_j < 1$, and $\sum_{j=1}^C \pi_j = 1$

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where $0 < \pi_j < 1$, and $\sum_{j=1}^C \pi_j = 1$

- More generally

$$f(y|\mathbf{x}; \mathbf{z}; \theta_1, \theta_2, \dots, \theta_C; \pi_1, \pi_2, \dots, \pi_C) = \sum_{j=1}^C \pi_j(\mathbf{z}) f_j(y|\mathbf{x}; \theta_j)$$

- Maximum likelihood

$$\max_{\pi, \theta} \ln L = \sum_{i=1}^N \left(\log \left(\sum_{j=1}^C \pi_j f_j(y | \theta_j) \right) \right)$$

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- Trick to ensure $0 < \pi_j < 1$, and $\sum_{j=1}^C \pi_j = 1$

$$\pi_j = \frac{\exp(\gamma_j)}{\exp(\gamma_1) + \exp(\gamma_2) + \dots + \exp(\gamma_{C-1}) + 1}$$

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- EM
- Bayesian MCMC

Model

Popular mixture component densities

- Normal (Gaussian)
- Poisson
- Gamma
- Negative Binomial
- Student-t
- Weibull

Model

Some basic properties

- Conditional mean:

$$E(y_i | \mathbf{x}_i) = \sum_{j=1}^C \pi_j \lambda_j \text{ where } \lambda_j = E_j(y_i | \mathbf{x}_i)$$

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- Marginal effects:

$$\frac{\partial E_j(y_i | \mathbf{x}_i)}{\partial \mathbf{x}_i} = \frac{\partial \lambda_j}{\partial \mathbf{x}_i} \longrightarrow \text{within component}$$

$$\frac{\partial E(y_i | \mathbf{x}_i)}{\partial \mathbf{x}_i} = \sum_{j=1}^C \pi_j \frac{\partial \lambda_j}{\partial \mathbf{x}_i} \longrightarrow \text{overall}$$

Model

Some basic properties

- Prior probability that observation y_i belongs to component c :

$$\Pr[y_i \in \text{population } c | \mathbf{x}_i, \boldsymbol{\theta}] = \pi_c$$

$$c = 1, 2, \dots, C$$

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$$\Pr[y_i \in \text{population } c | \mathbf{x}_i, \boldsymbol{\theta}] = \pi_c$$

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- Posterior probability that observation y_i belongs to component c :

$$\Pr[y_i \in \text{population } c | \mathbf{x}_i, y_i, \boldsymbol{\theta}] = \frac{\pi_c f_c(y_i | \mathbf{x}_i, \boldsymbol{\theta}_c)}{\sum_{j=1}^C \pi_j f_j(y_i | \mathbf{x}_i, \boldsymbol{\theta}_j)}$$

$$c = 1, 2, \dots, C$$

- The number of components has to be specified - we usually have little theoretical guidance
- Even if prior theory suggests a particular number of components we may not be able to reliably distinguish between some of the components
- In some cases additional components may simply reflect the presence of outliers in the data
- Likelihood function may have multiple local maxima

- Parameterize $\gamma_j = Z\alpha_j$ in

$$\pi_j = \frac{\exp(\gamma_j)}{\exp(\gamma_1) + \exp(\gamma_2) + \dots + \exp(\gamma_{C-1}) + 1}$$

- Parameterizing mixing probabilities
 - may lead to finite sample identification issues
 - may lead to computational difficulties

Model

Selecting number of components

- Estimate models with 2 and then more components
- At each step calculate

$$AIC = -2 \log(L) + 2K$$

$$BIC = -2 \log(L) + K \log(N)$$

- Pick the model with the smallest AIC , BIC

- Stata package `fmm`

```
fmm depvar [indepvars] [if] [in] [weight],  
components(#) mixtureof(density)
```

- where density is one of

```
gamma  
negbin1  
negbin2  
normal  
poisson  
studentt
```

- `predict` and `mfx` give predictions and marginal effects of means, component means, prior and posterior probabilities

Applications

Infant Birthweight and Prenatal Care

- Expanding prenatal care should improve infant health!
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- Research using observational data typically finds weak, if any, effects

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- Expanding prenatal care should improve infant health!
- Clinical interventions show positive effects
- Research using observational data typically finds weak, if any, effects

- Why?
 1. difficulties in measuring prenatal care
 2. difficulties in modeling its endogeneity
 3. there are essentially two kinds of pregnancies, “complicated” and “normal” ones

Applications

Infant Birthweight and Prenatal Care

- Study of the effect of the onset (timing) of prenatal care on birthweight

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- Study of the effect of the onset (timing) of prenatal care on birthweight
- Complicated pregnancies typically entail a large amount of prenatal care, but yield poorer outcomes
- Clinical evidence suggests that such births are quite difficult to prevent
- Observed factors such as prenatal care and other maternal behaviors may have different effects on each type of pregnancy
- Combining these pregnancies with normally progressing pregnancies could lead prenatal care to appear ineffective

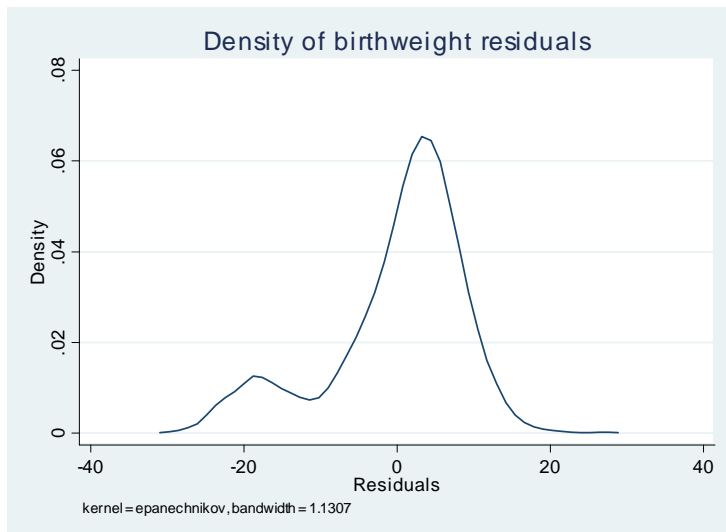
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- Econometric strategy: Use a finite mixture model

- Data from the National Maternal and Infant Health Survey
 - Contains information on 26,355 women who were pregnant in 1988
 - Oversamples fetal deaths and infant deaths
 - Oversamples blacks and low birthweight babies
 - Sample of singleton live births:
 - 3,350 nonHispanic blacks
 - 3,245 nonHispanic whites
- Number of observations: 5,219
- Number of covariates: 12

Applications

Infant Birthweight and Prenatal Care



Applications

Infant Birthweight and Prenatal Care

Variable	Parameter estimates		
	OLS	FMM	
		component 1	component 2
onsethat	-0.501** (0.183)	-0.294* (0.127)	0.006 (0.234)

Applications

Infant Birthweight and Prenatal Care

Variable	Parameter estimates		
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onsethat	-0.501** (0.183)	-0.294* (0.127)	0.006 (0.234)
black	-1.213** (0.312)	-1.231** (0.215)	-0.775* (0.393)

Applications

Infant Birthweight and Prenatal Care

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onsethat	-0.501** (0.183)	-0.294* (0.127)	0.006 (0.234)
black	-1.213** (0.312)	-1.231** (0.215)	-0.775* (0.393)
edu	0.353** (0.074)	0.292** (0.050)	0.040 (0.102)

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numdead	-1.181** (0.163)	-0.170 (0.117)	-0.585** (0.171)

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numdead	-1.181** (0.163)	-0.170 (0.117)	-0.585** (0.171)
π		0.864	0.136
se(π)		(0.005)	(0.005)

Applications

Infant Birthweight and Prenatal Care

- Remarkable robustness of the finite mixture model across samples, races and weighting schemes

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- Clear message – getting prenatal care one week earlier significantly increases birth weights in 'normal' pregnancies by 30-50 grams per week

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- Estimated probability of having a 'normal' pregnancy is 0.856 to 0.873 across samples, races and weighting schemes

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Infant Birthweight and Prenatal Care

- Remarkable robustness of the finite mixture model across samples, races and weighting schemes
- Clear message – getting prenatal care one week earlier significantly increases birth weights in 'normal' pregnancies by 30-50 grams per week
- Estimated probability of having a 'normal' pregnancy is 0.856 to 0.873 across samples, races and weighting schemes
- Estimated magnitudes are on target with the medical literature

- Study of the price (insurance) elasticity of demand for healthcare services

- Study of the price (insurance) elasticity of demand for healthcare services
- The two-part model (TPM) is the methodological cornerstone of empirical analysis in the analysis of medical care use
 - “... the decision to receive some care is largely the consumer’s, while the physician influences the decision about the level of care” (Manning et al. 1981, p. 109)
 - “... while at the first stage it is the patient who determines whether to visit the physician, it is essentially up to the physician to determine the intensity of the treatment” (Pohlmeier and Ulrich, 1995, p. 340)
 - “...where the first part relates to the patient who decides whether to contact the physician and the second to the decision about repeated visits and/or referrals, which is determined largely by the preferences of the physician” (Gerdtham, 1997, p. 308)

- The sharp dichotomy between users and nonusers may not be tenable in the case of typical cross-sectional data-sets

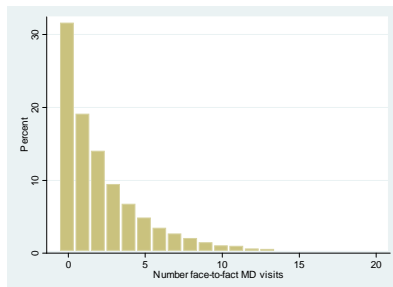
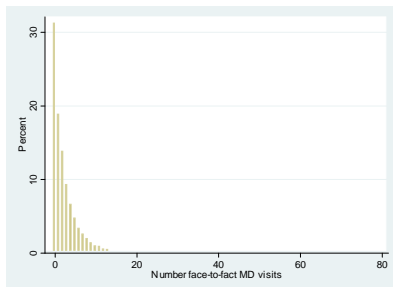
- The sharp dichotomy between **users** and **nonusers** may not be tenable in the case of typical cross-sectional data-sets
- A better distinction for such data may be between **infrequent users** and **frequent users** of medical care

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- A better distinction for such data may be between **infrequent users** and **frequent users** of medical care
- The finite mixture model provides a better framework for distinguishing between infrequent and frequent users

- Data from the Rand Health Insurance Experiment (RHIE)
 - conducted by the RAND Corporation from 1974 to 1982
 - individuals were randomized into insurance plans
 - widely regarded as the basis of the most reliable estimates of price elasticities
 - collected from about 8,000 enrollees in 2,823 families from six sites across the country
 - each family was enrolled in one of fourteen different insurance plans for either three or five years
 - the FFS plans ranged from free care to 95 % coinsurance
- Data from all 5 years of the experiment
- Number of observations: 20,186
- Number of covariates: 17

Applications

Medical Care Use



Explanatory variables

LC	$\ln(\text{coinsurance}+1)$, $0 \leq \text{coinsurance} \leq 100$
IDP	1 if individual deductible plan, 0 otherwise
LPI	f(annual participation incentive payment)
FMDE	f(maximum dollar expenditure)
LINC	$\ln(\text{family income})$
LFAM	$\ln(\text{family size})$
EDUCDEC	education of the household head in years
PHYSLIM	1 if the person has a physical limitation
NDISEASE	number of chronic diseases
HLTHG, F, P	self-rated health

AGE, FEMALE, CHILD, FEMALE * CHILD, BLACK

- The density of the C -component finite mixture is specified as

$$f(y_i | \theta_1, \theta_2, \dots, \theta_C; \pi_1, \pi_2, \dots, \pi_C) \\ = \sum_{j=1}^C \pi_j \frac{\Gamma(y_i + \psi_{j,i})}{\Gamma(\psi_{j,i})\Gamma(y_i + 1)} \left(\frac{\psi_{j,i}}{\lambda_{j,i} + \psi_{j,i}} \right)^{\psi_{j,i}} \left(\frac{\lambda_{j,i}}{\lambda_{j,i} + \psi_{j,i}} \right)^{y_i}$$

where $\lambda = \exp(x\beta)$ and $\psi = (1/\alpha)\lambda^k$

- $k = 1$ NB-2
- $k = 0$ NB-1
- $k = 0$ fits best

Applications

Medical Care Use

Parameter Estimates			
	nb1	fmm nb1	
		component 1	component 2
logc	-0.149*	-0.203*	-0.024
	(0.012)	(0.020)	(0.031)

	Parameter Estimates		
	nb1	fmm nb1	
		component 1	component 2
logc	-0.149* (0.012)	-0.203* (0.020)	-0.024 (0.031)
educdec	0.023* (0.003)	0.027* (0.005)	0.015 (0.010)

Parameter Estimates

	nb1	fmm nb1	
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logc	-0.149* (0.012)	-0.203* (0.020)	-0.024 (0.031)
educdec	0.023* (0.003)	0.027* (0.005)	0.015 (0.010)
disea	0.021* (0.001)	0.019* (0.002)	0.033* (0.004)

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logc	-0.149*	-0.203*	-0.024
	(0.012)	(0.020)	(0.031)
educdec	0.023*	0.027*	0.015
	(0.003)	(0.005)	(0.010)
disea	0.021*	0.019*	0.033*
	(0.001)	(0.002)	(0.004)
π		0.802	0.198
		(0.037)	(0.037)
log L	-42405	-42037	
BIC	84999	84461	

Applications

Medical Care Use

Marginal Effects

	nb1		fmm nb1	
	overall	overall	component 1	component 2
$E(y \bar{x})$	2.561	2.511	1.887	5.038
logc	-0.382*	-0.331*	-0.382*	-0.121
	(0.030)	(0.032)	(0.032)	(0.158)

Applications

Medical Care Use

Marginal Effects

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$E(y \bar{x})$	2.561	2.511	1.887	5.038
logc	-0.382* (0.030)	-0.331* (0.032)	-0.382* (0.032)	-0.121 (0.158)
educdec	0.058* (0.007)	0.056* (0.009)	0.052* (0.008)	0.073 (0.053)

Applications

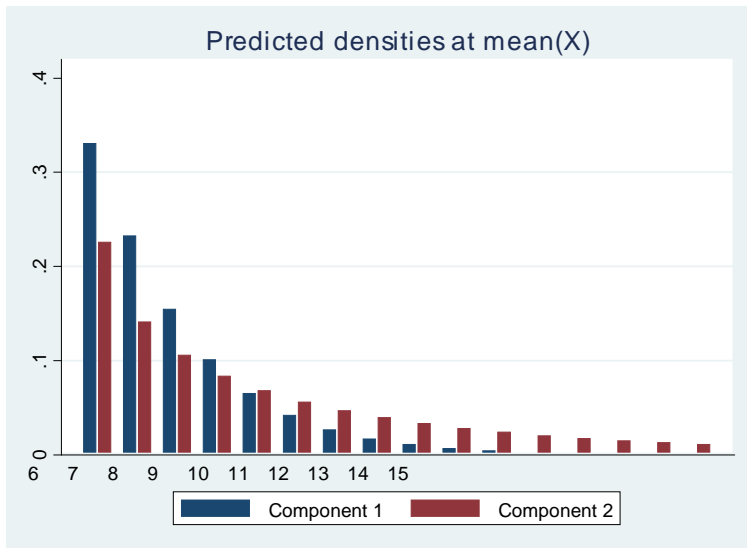
Medical Care Use

Marginal Effects

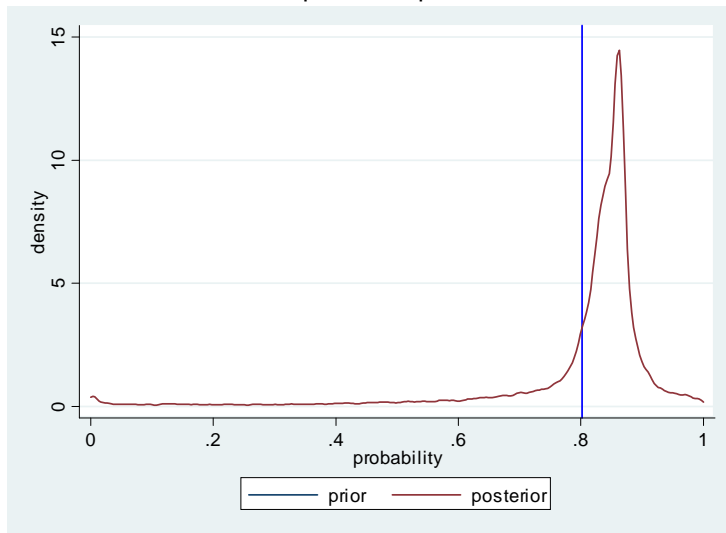
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logc	-0.382* (0.030)	-0.331* (0.032)	-0.382* (0.032)	-0.121 (0.158)
educdec	0.058* (0.007)	0.056* (0.009)	0.052* (0.008)	0.073 (0.053)
disea	0.054* (0.003)	0.062* (0.004)	0.036* (0.004)	0.167* (0.024)

Applications

Medical Care Use



Prior and posterior probabilities



Applications

Job loss, BMI and drinking

- Study of effects of business closures on alcohol use and body mass index (BMI)

Applications

Job loss, BMI and drinking

- Study of effects of business closures on alcohol use and body mass index (BMI)
- Job loss frequently involves a succession of stress-laden experiences
- Evidence on the health effects of job loss is mixed
- Evidence on changes in weight associated with unemployment is similarly ambiguous
- Evidence on the effects of job loss on mental health status is more definitive

Applications

Job loss, BMI and drinking

- There is wide variation in the individual behavioral response to the stress of job loss
- Greater alcohol or food consumption could conceivably counterbalance neuro- or emotion-regulatory disturbances
- But unemployment introduces discretionary time which may be used to pursue health-promoting behaviors
- Income losses could constrain job losers to certain food choices or limit alcohol purchases

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- Econometric strategy: Use a finite mixture model

Applications

Job loss, BMI and drinking

- Job loss has frequently been represented by layoff or some combination of involuntary termination (e.g., layoff, plant closing, and firing)
- Layoffs and firing are likely to be endogenous
- We use business closing

Applications

Job loss, BMI and drinking

- Data from the Health and Retirement Study (HRS)
 - 12,652 individuals from 7,702 households at baseline
- Data from the first six HRS waves (1992-2002)
- Analysis sample restricted to participants who met the following criteria at the 1992 baseline
 1. were between ages 51 and 61
 2. were working for pay, but not self employed
 3. reported a minimum of two years of continuous employment with the 1992 employer
 4. provided at least one follow-up response
- Limit the sample to study subjects who reported continuous employment in the previous person-spell
- Number of observations: 6,726.

Applications

Job loss, BMI and drinking

Variable	Parameter estimates		
	OLS	FMM Normal component1	component2
Business closure	0.081 (0.149)	-0.192 (0.119)	1.083** (0.541)

Applications

Job loss, BMI and drinking

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π		0.806*** (0.026)	

Applications

Job loss, BMI and drinking

Variable	Parameter estimates		
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Business closure	0.228 (0.173)	0.131 (0.109)	0.844*** (0.242)

Applications

Job loss, BMI and drinking

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Business closure	0.228 (0.173)	0.131 (0.109)	0.844*** (0.242)
Non-housing net worth	0.082*** (0.028)	0.119*** (0.034)	-0.211 (0.172)

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Job loss, BMI and drinking

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Lagged number of drinks	1.587*** (0.040)	1.986*** (0.067)	0.191 (0.189)

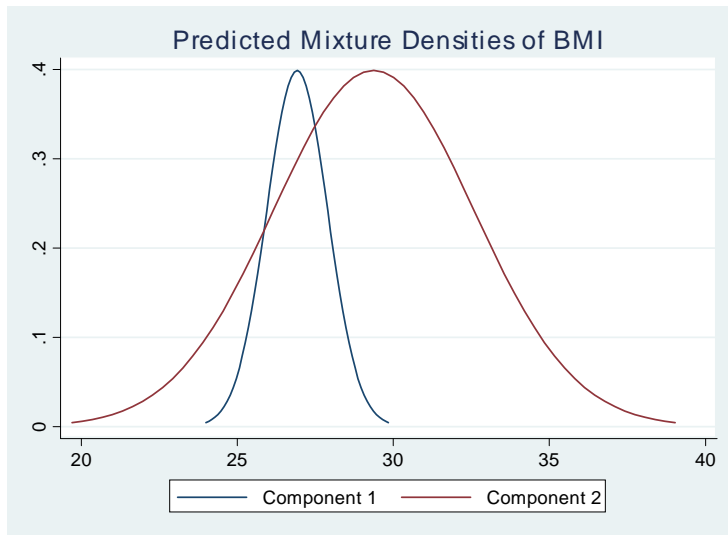
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π			0.939*** (0.009)

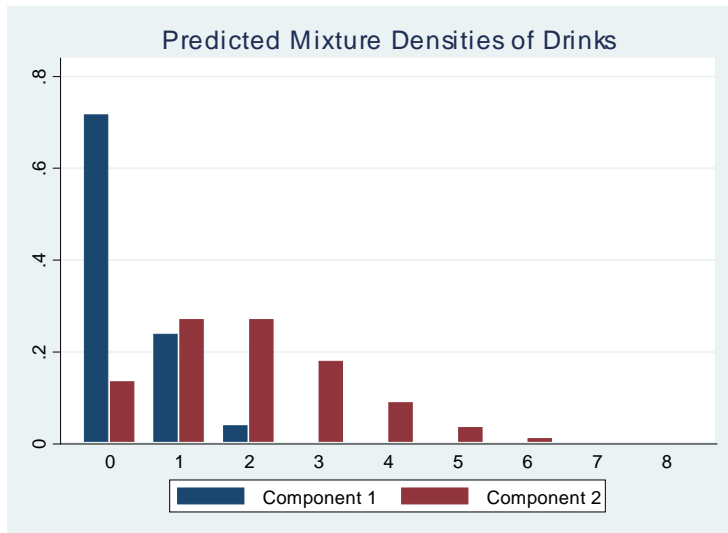
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Applications

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Applications

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Determinants of posterior probability of being in component 2: BMI

Variable	(1)	(2)	(3)
Married	-0.007 (0.008)	-0.000 (0.008)	0.000 (0.008)
Non-housing net worth	-0.019*** (0.004)	-0.017*** (0.005)	-0.017*** (0.005)
Depressive symptoms	0.011*** (0.003)	0.010*** (0.003)	0.010*** (0.004)
Non-white		0.017* (0.010)	0.017* (0.010)
Male		-0.025*** (0.007)	-0.025*** (0.007)
Risk averse	0.004 (0.004)	0.003 (0.004)	0.003 (0.004)

Applications

Job loss, BMI and drinking

Determinants of posterior probability of being in component 2: Drinks

Variable	(1)	(2)	(3)
Married	-0.004 (0.006)	-0.012** (0.006)	-0.012** (0.006)
Non-housing net worth	0.006* (0.003)	0.006 (0.004)	0.006* (0.004)
Depressive symptoms score	-0.001 (0.003)	-0.001 (0.003)	-0.001 (0.003)
Non-white		-0.007 (0.007)	-0.007 (0.007)
Male		0.032*** (0.006)	0.033*** (0.006)
Risk averse	-0.007** (0.003)	-0.006** (0.003)	-0.006** (0.003)

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